

Di

(1)

Graphene 的对称性

π -flux 的为什么会有 Dirac cone?



• Unconventional superconductivity

$$\Psi_{\alpha_1, \alpha_2}(r_1, r_2) = \Phi(\vec{R}) \phi(\vec{r}_1 - \vec{r}_2) \chi_{\alpha_1, \alpha_2}$$

$$\Phi(\vec{R}) = e^{i\vec{k} \cdot \vec{R}} \quad - \text{PDW}$$

isotropic system: $\phi(\vec{r}_1 - \vec{r}_2) = Y_{lm}(r) R(r)$

就是在动量有限大的地方配对

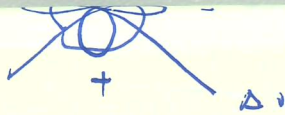
• $R_n(r)$ has nodes - extended s wave

1. conventional superconductivity: $R_{n=0}(r)$

positive-definite: ~~comp~~ wavefunction 不变的

d-wave superconductivity

$$\phi(\vec{r}) = \sum_{\vec{k}} e^{i\vec{k} \cdot \vec{r}} \Delta(\vec{k})$$



$$\Delta(\phi) = \Delta_d \cos(2\phi)$$

- Fractional superconductivity:

$$\Delta(\phi) \propto \cos(\alpha\phi)$$

- p-wave ^3He A-B phases:

$$l = 1, \quad p_x, p_y, p_z$$

$$s = 1, \quad \uparrow$$

$$\Delta_{\alpha\beta}(k) = \sum_{k'} g(k-k') C_{k'\alpha}^\dagger \left(i\sigma_2 \sigma^\alpha \right)_{\alpha\beta}$$

$$k' \alpha \quad k' C_{k'\beta}$$

Singlet pairing:

$$\boxed{C_\alpha^\dagger (i\sigma_2) C_\beta^\dagger}$$

anti-symmetric $(i\sigma_2 \sigma_\alpha)$

charge conjugation matrix

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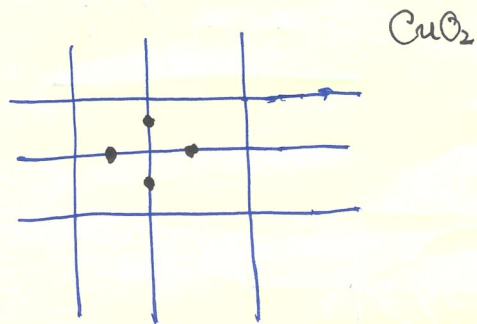
本产品适合14周岁以下(含14周岁)的学生使用, 14周岁以上也可使用



$$(\sigma_z c^\dagger) = \begin{pmatrix} c_\uparrow^\dagger \\ -c_\uparrow^\dagger \end{pmatrix} = \begin{pmatrix} c_\uparrow \\ c_\downarrow \end{pmatrix}$$

• $\psi (\sigma_y \otimes \sigma_y)$

• Cuprate:



$$H_0 = -t \sum_{\langle i,j \rangle} c_i^\dagger c_j + h.c. - \mu \sum c_{i\sigma}^\dagger c_{i\sigma}$$

$$H_{int} = -\frac{V}{2} \sum_{\delta=\pm\hat{x}} (c_{i+\delta\downarrow}^\dagger c_{i\uparrow} - c_{i+\delta\uparrow}^\dagger c_{i\downarrow}^\dagger)$$

$$(c_{i\uparrow}^\dagger c_{i+\delta\downarrow} - c_{i\downarrow}^\dagger c_{i+\delta\uparrow})$$

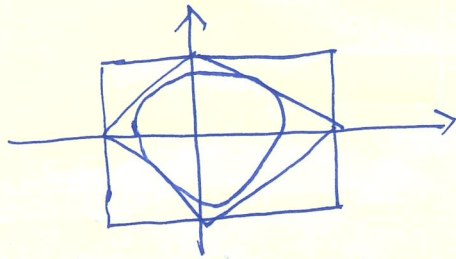
↓
不同 site 之间的 pairing:

phenomenological interaction

Hydride

$$\text{if: } \mu = 0, \quad \epsilon_k = 0, \quad \langle n_k \rangle = C_{k\sigma}^\dagger C_{k\sigma} = 1$$

$$H \sim H : \quad \underline{C_j - (-1)^n C_j}$$



$$\boxed{\cos k_x + \cos k_y - \mu = 0}$$

$$H_{\text{pair}} = -\frac{v}{\Omega N} \sum (C_{-k\downarrow}^\dagger C_{k'\uparrow} - C_{-k'\uparrow}^\dagger C_{k\downarrow})$$

$$(C_{k'\uparrow} C_{-k\downarrow} - C_{-k'\uparrow} C_{k\downarrow}) e^{v(k'\cdot\sigma - k\cdot\sigma)}$$

$$= -\frac{v}{\Omega N} \sum_{k, k'} \underline{4(\cos k_x \cos k_x + \cos k_y \cos k_y)}$$

$$\underline{C_{-k'\downarrow}^\dagger C_{k'\uparrow}^\dagger C_{k\uparrow} C_{-k\downarrow}}$$

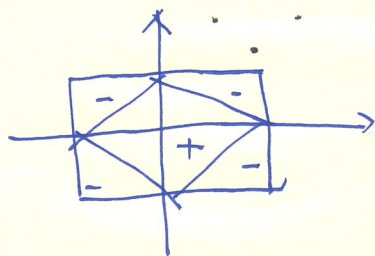


$$= -\frac{V}{N} \sum_{\mathbf{k}, \mathbf{k}'} \left\{ (\cos k_x \mp \cos k_y) (\cos k'_x - \cos k'_y) \right. \quad (5)$$

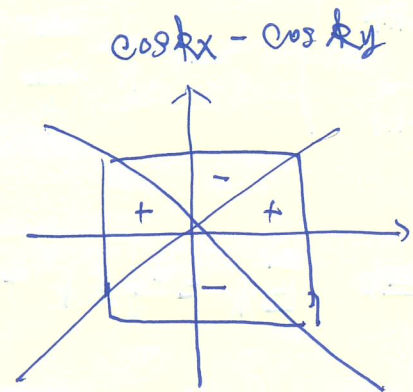
$$+ \left. (\cos k_x + \cos k_y) (\cos k'_x + \cos k'_y) \right\} C_{-\mathbf{k}'\downarrow}^+ C_{\mathbf{k}\uparrow}^+ C_{\mathbf{k}\uparrow}$$

square
 $C_{\mathbf{k}\downarrow}$

分解成 s 波和 d 波



$\cos k_x + \cos k_y$



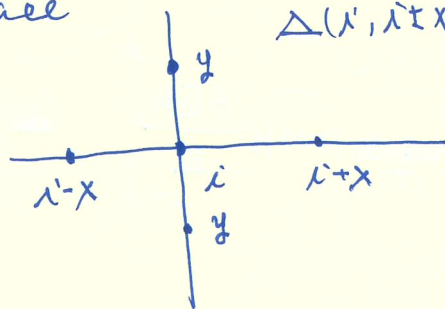
$\cos k_x - \cos k_y$

$$\frac{1}{N} H_{MF} = -\frac{V}{N} \sum_{\mathbf{k}} \left\{ \Delta_s^* (\cos k_x + \cos k_y) \right.$$

$$C_{\mathbf{k}\uparrow} C_{-\mathbf{k}\downarrow} + h.c. + \Delta_d^* (\cos k_x - \cos k_y) C_{\mathbf{k}\uparrow} C_{-\mathbf{k}\downarrow}$$

$$\left. + h.c. \right\} + \frac{1}{V} (\Delta_s^* \Delta_s + \Delta_d^* \Delta_d)$$

Real space



$$\Delta(\mathbf{r}, \mathbf{r} \pm \mathbf{x}) = \Delta(\mathbf{r}, \mathbf{r} \pm \mathbf{y})$$

of $\int C d\mathbf{k} \sinh \frac{\beta E_{\mathbf{k}}}{2}$

Δ_d

⑦

⑥

$$\Delta(N, i \pm x) = -\Delta(N, i \pm y)$$

singlet pairing 出现 s 波配对

$$\frac{H}{N} = \frac{1}{N} \sum_{\mathbf{k}} (C_{\mathbf{k}\uparrow}^\dagger \ C_{-\mathbf{k}\downarrow}) \begin{pmatrix} \epsilon_{\mathbf{k}} - \mu & \Delta_d (\cos k_x - \cos k_y) \\ \Delta_d (\cos k_x - \cos k_y) & -(\epsilon_{\mathbf{k}} - \mu) \end{pmatrix}$$

$$\begin{pmatrix} C_{\mathbf{k}\uparrow} \\ C_{-\mathbf{k}\downarrow}^\dagger \end{pmatrix} + \frac{1}{N} \sum_{\mathbf{k}} (\epsilon_{\mathbf{k}} - \mu) + \frac{1}{N} \Delta_d^* \Delta_d$$

$$\Rightarrow \bar{E}_{\mathbf{k}} = \pm \sqrt{\frac{v}{s} k^2 + \Delta_{\mathbf{k}}^2}$$

$$\Rightarrow \frac{1}{N} \sum_{\mathbf{k}} \bar{E}_{\mathbf{k}} (\alpha_{\mathbf{k}\uparrow}^\dagger \alpha_{\mathbf{k}\uparrow} - 1/2) + (\beta_{-\mathbf{k}\downarrow}^\dagger \beta_{-\mathbf{k}\downarrow} - 1/2)$$

Self-consistency eq:

$$\frac{F}{N} = - \frac{1}{V} \sum_{\mathbf{k}} \frac{2}{\beta} \log \left(e^{\frac{\beta}{2} \bar{E}_{\mathbf{k}}} + e^{-\frac{\beta}{2} \bar{E}_{\mathbf{k}}} \right)$$

occupy unoccupy
 \downarrow \downarrow

$$+ \frac{|\Delta_d|^2}{V}$$

$$\Rightarrow \frac{F}{N} = - \frac{2}{\beta} \int \frac{d\mathbf{k}}{(2\pi)^2} \log 2 \cosh \frac{\beta E_{\mathbf{k}}}{2} + \frac{|\Delta_d|^2}{V}$$

$$\frac{\partial F}{\partial \Delta} = -\frac{2}{B} \int \frac{d^2k}{(2\pi)^2} \frac{\sinh \frac{\beta E_k}{2}}{\cosh \frac{\beta E_k}{2}} \frac{\Delta d}{2\sqrt{\xi_k^2 + \Delta^2}} \quad (7)$$

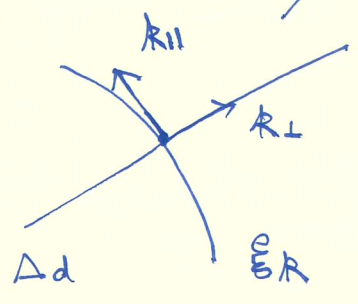
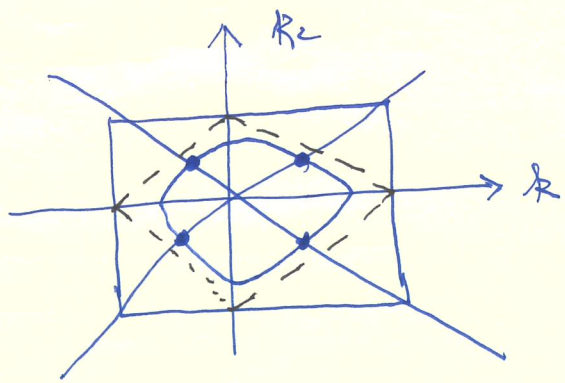
$$(\cos k_x - \cos k_y)^2 + \frac{2\Delta d}{v} = 0$$

$$\Delta d = v \int \frac{d^2k}{(2\pi)^2} \tan \frac{\beta E_k}{2} \frac{\Delta d}{E_k} (\cos k_x - \cos k_y)^2$$

↓ iteration

• Excitation : $E_k = \sqrt{\xi_k^2 + \Delta^2(k)}$

nodal particles: $E_k = 0; \xi_k = \Delta(k) = 0$



$$H(k) = \begin{pmatrix} \xi(k) & \Delta(k) \\ \Delta(k) & -\xi(k) \end{pmatrix}$$

$$= \hbar v_F \xi_{kL} \tau_z + \Delta d \xi_{kll} \tau_x$$

d 波的 nodal ~~line~~ 就是 Dirac cone pin